

Maximum Wireless Power Extraction: Some Antennas in the Receive Array May Have to Transmit Power

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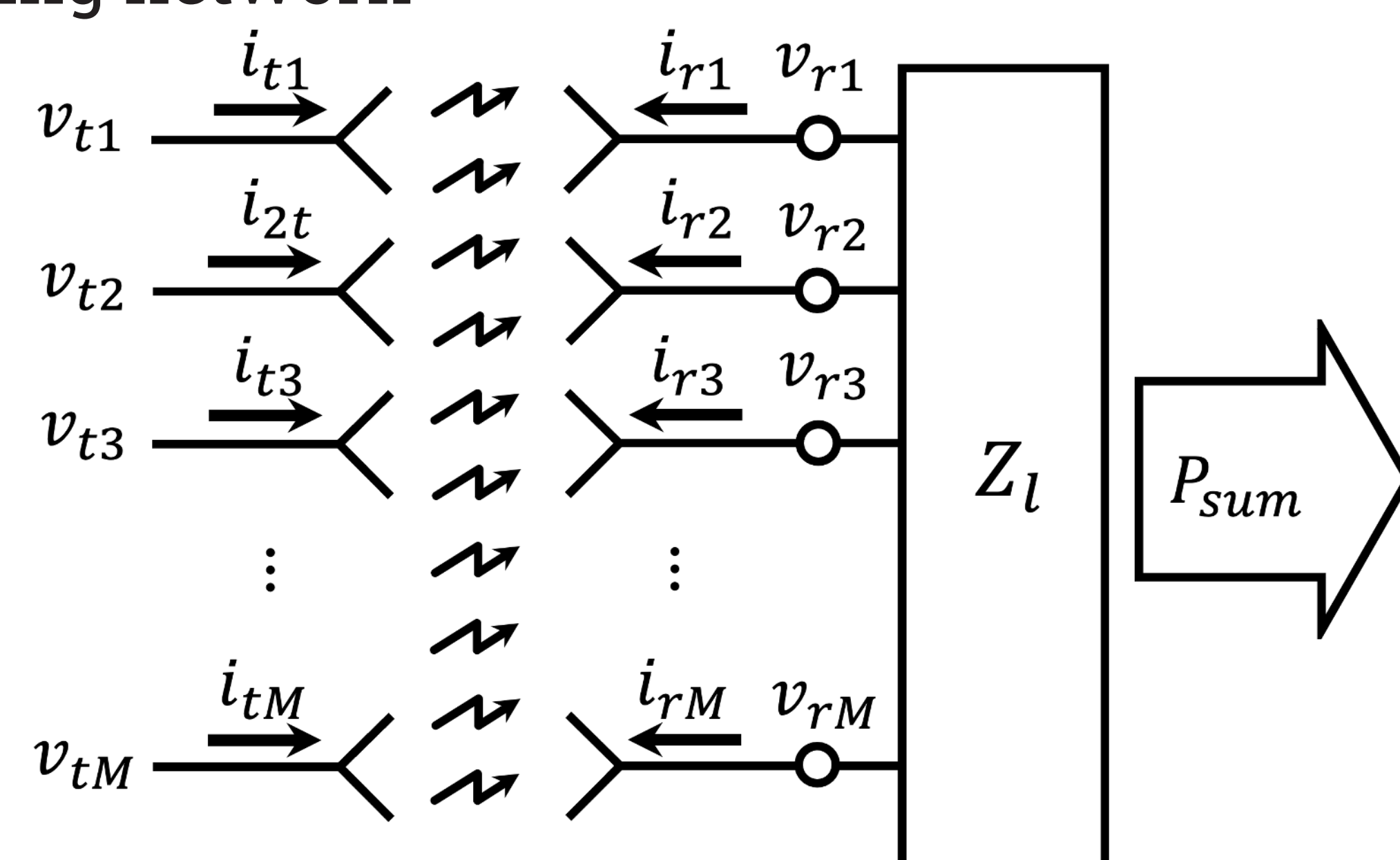
BACKGROUND

Current wireless power transfer technology is relegated to short range and low power. Super-directivity hold out hope for powering a drone 100 meters away, with a physically small transmit array, but the concept has never been reduced to practice [3]

- Portable electronics provide substantial demand
- New wireless power infrastructure must consider spectrum usage
- The physics is old, but still not completely understood

MAXIMUM WIRELESS POWER TRANSFER

A wireless power transfer system is usually defined with a transmit and receive array, each with a matching network



We can treat each array as a ported network [2]:

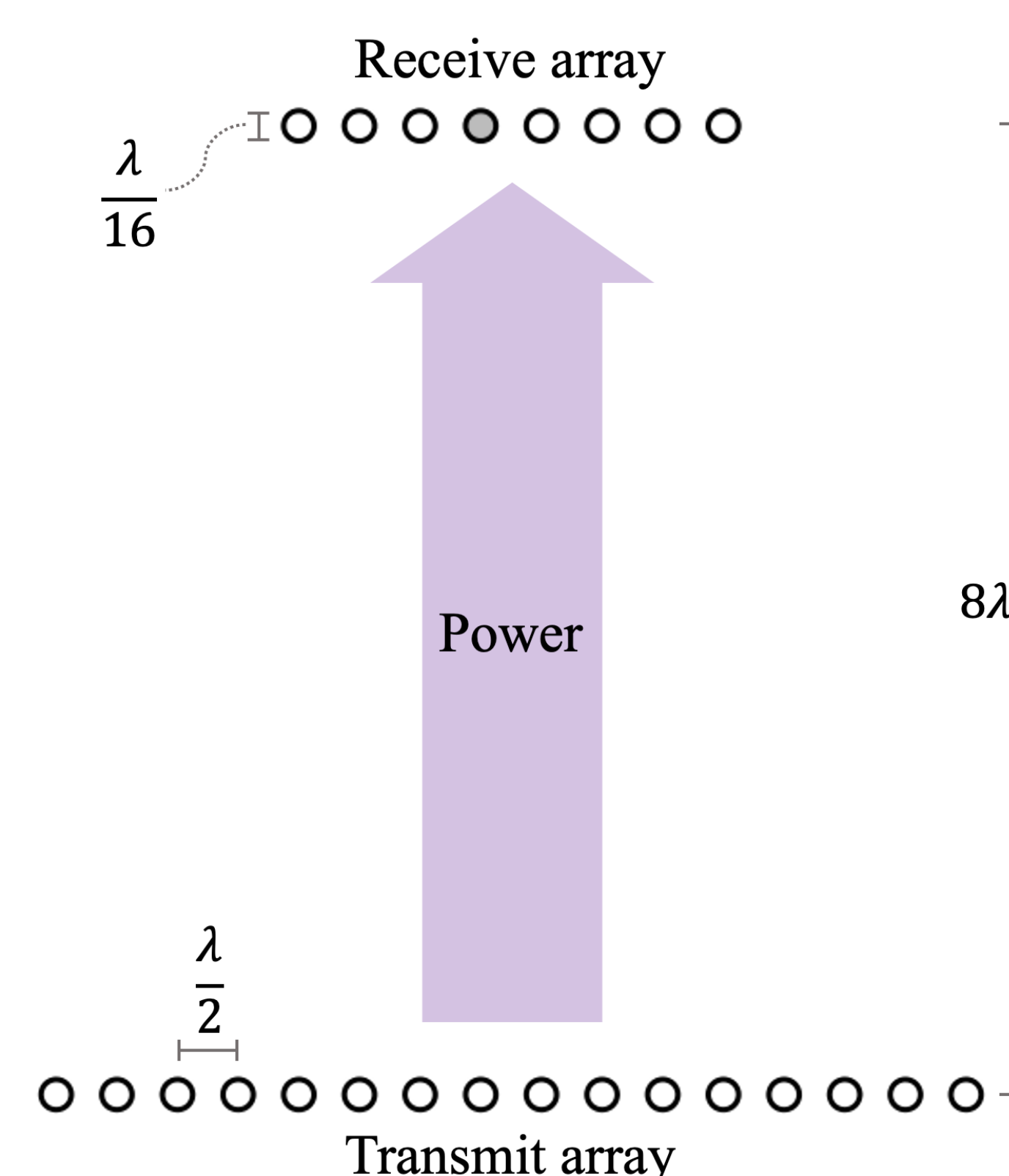
$$\begin{bmatrix} \mathbf{v}_T \\ \mathbf{v}_R \end{bmatrix} = \begin{bmatrix} \mathbf{Z}_T & \mathbf{Z}_{TR}^T \\ \mathbf{Z}_{TR} & \mathbf{Z}_R \end{bmatrix} \begin{bmatrix} \mathbf{i}_T \\ \mathbf{i}_R \end{bmatrix}$$

We pull maximum sum-power out of the receive array. We show that, in so doing, one of the antennas may radiate positive power.

$$\min_{\mathbf{i}_T} \frac{P_{R1}}{P_{sum}} = \min_{\mathbf{v}_{OC}} \frac{0.5 \text{Re}[\mathbf{i}_{R1}^* \mathbf{v}_{R1}]}{.125 \mathbf{v}_{OC}^H \text{Re}[\mathbf{Z}_R]^{-1} \mathbf{v}_{OC}}$$

And we solve the resulting eigenvector/eigenvalue problem.

NUMERICAL SIMULATION OF SYSTEM



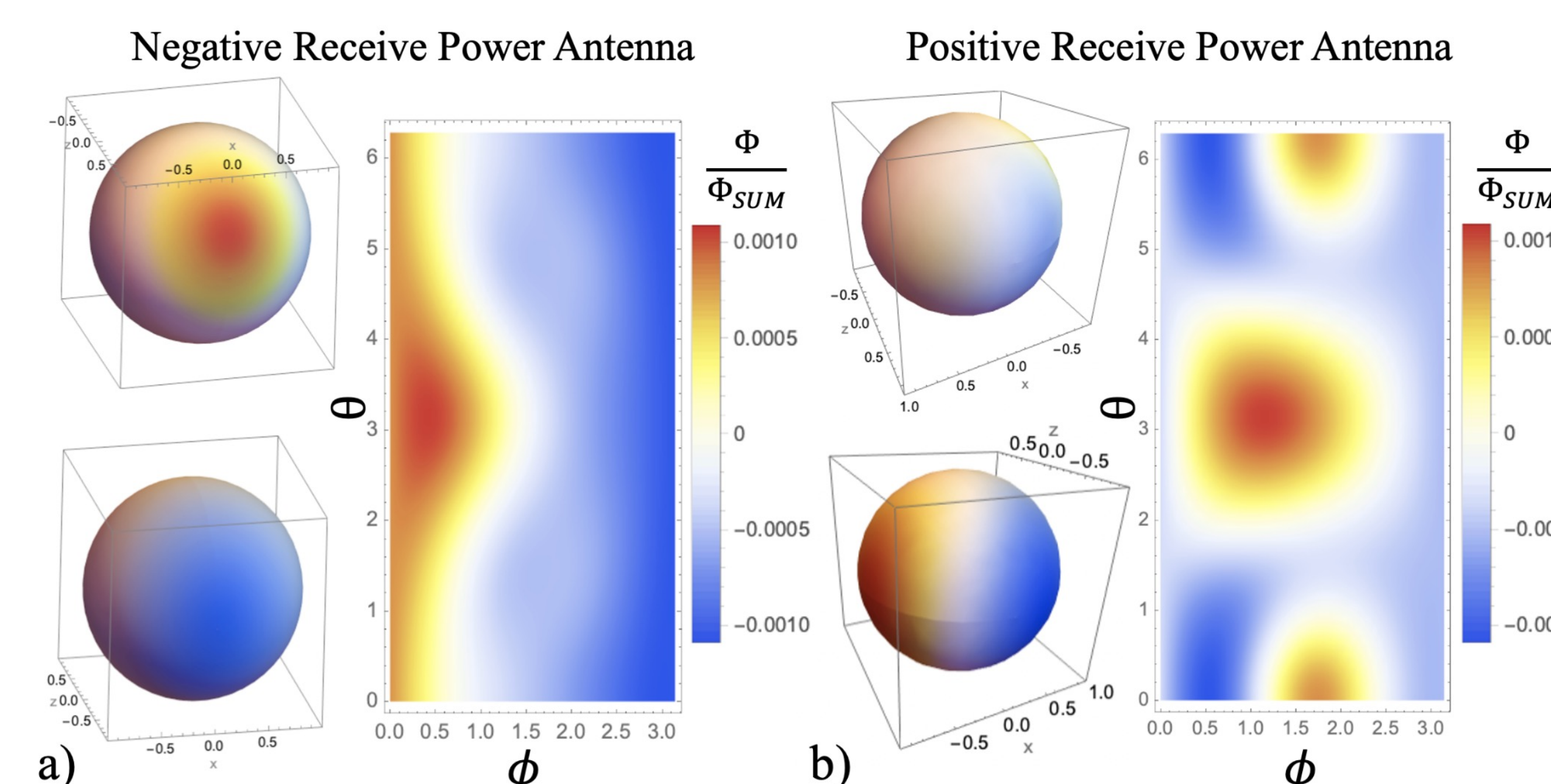
- We perform simulations using $\frac{\lambda}{2}$ -spaced antenna arrays
- The antenna radiating positive power is marked in grey
- Using an LTI acoustic model, we populate the impedance matrix [3]:

$$Z_{self} = 1 - i \frac{\cos(kR_0)}{\sin(kR_0)}$$

$$Z_{mut}(R) = \frac{\sin(kR)}{kR} - i \frac{\cos(kR)}{kR}$$

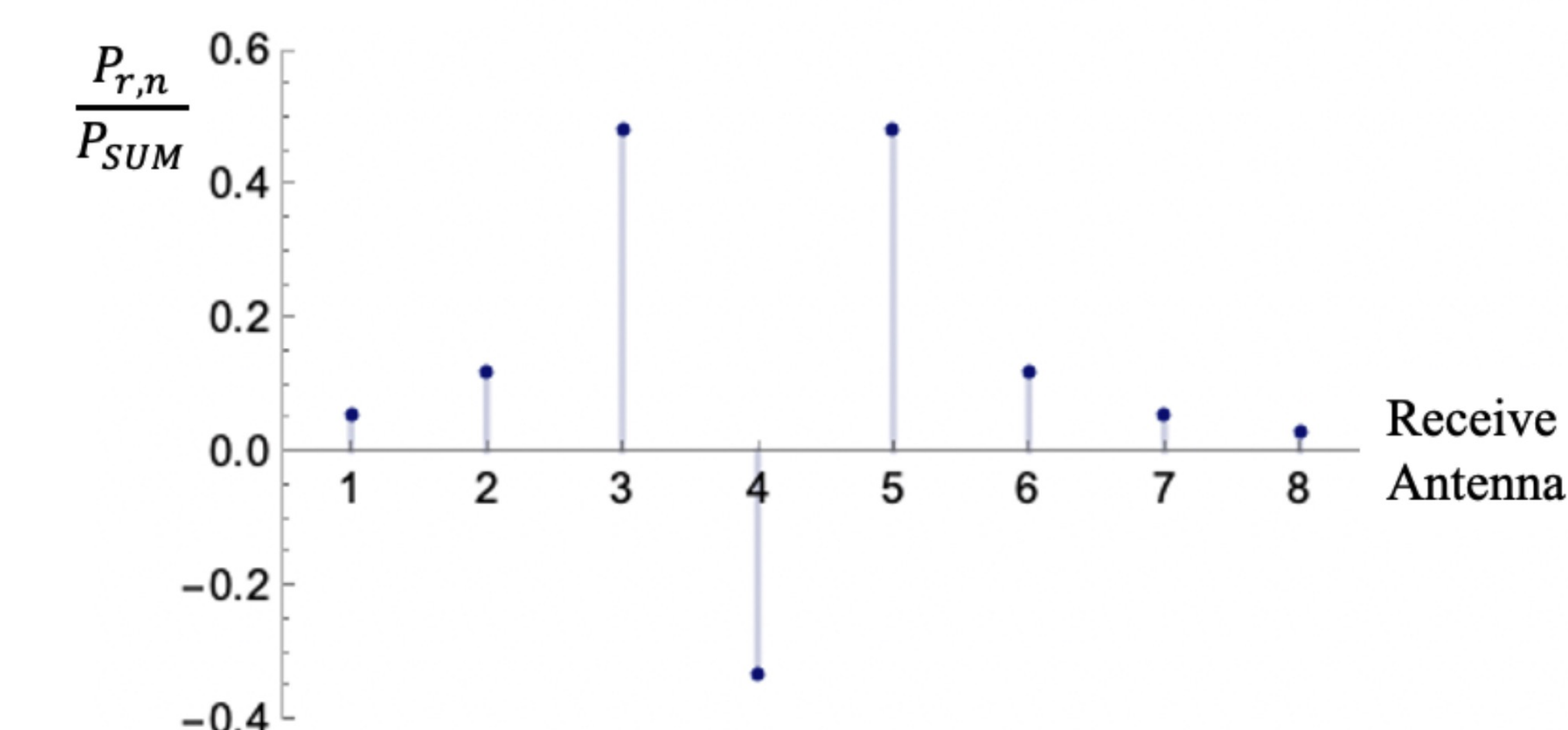
RESULT: ANTENNA COUPLING EFFECTS

We can simulate the surface flux on each of the antennas using our acoustic model:



- The radiating receive antenna (a) mostly receives power from the transmit array direction
- An adjacent antenna that absorbs power (b) can be seen receiving power in the direction of the radiating antenna
- This implies the radiating antenna is actively assisting other antennas in the array

RESULT: POWER ON EACH ANTENNA



- Here a plot of the power received by each antenna is normalized by the sum-power
- The sum power diminishes as distance from the radiating antenna increases, showing the role the radiating antenna plays in max power transfer

ACKNOWLEDGEMENTS

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